



VOLUME XI
ISBN No.: 978-93-94004-00-9
Physical Science

NALLAMUTHU GOUNDER MAHALINGAM COLLEGE

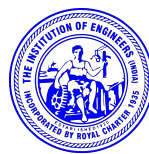
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One day International Conference

EMERGING TRENDS IN SCIENCE AND TECHNOLOGY (ETIST-2021)

27th October 2021

Jointly Organized by

Department of Biological Science, Physical Science and Computational Science

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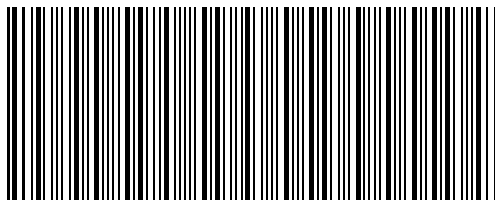
Proceeding of the
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ABOUT THE INSTITUTION

A nation's growth is in proportion to education and intelligence spread among the masses. Having this idealistic vision, two great philanthropists late. S.P. Nallamuthu Gounder and Late. Arutchelver Padmabhushan Dr.N.Mahalingam formed an organization called Pollachi Kalvi Kazhagam, which started NGM College in 1957, to impart holistic education with an objective to cater to the higher educational needs of those who wish to aspire for excellence in knowledge and values. The College has achieved greater academic distinctions with the introduction of autonomous system from the academic year 1987-88. The college has been Re-Accredited by NAAC and it is ISO 9001 : 2015 Certified Institution. The total student strength is around 6000. Having celebrated its Diamond Jubilee in 2017, the college has blossomed into a premier Post-Graduate and Research Institution, offering 26 UG, 12 PG, 13 M.Phil and 10 Ph.D Programmes, apart from Diploma and Certificate Courses. The college has been ranked within Top 100 (72nd Rank) in India by NIRF 2021.

ABOUT CONFERENCE

The International conference on “Emerging Trends in Science and Technology (ETIST-2021)” is being jointly organized by Departments of Biological Science, Physical Science and Computational Science - Nallamuthu Gounder Mahalingam College, Pollachi along with ISTE, CSI, IETE, IEE & RIYASA LABS on 27th OCT 2021. The Conference will provide common platform for faculties, research scholars, industrialists to exchange and discuss the innovative ideas and will promote to work in interdisciplinary mode.

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A note on soft αgrw -closed sets

N. Selvanayaki¹, Gnanambal Ilango² and M.Maheswari³,

Abstract - Aim of this paper is to study some properties of αgrw -closed sets in soft topological spaces and related characterizations are studied.

Keywords *Soft sets, soft topological spaces, soft αgrw -closed sets and soft regular semi kernal.*

2010 Subject classification: *54A05, 54A10.*

1 Introduction and Preliminaries

Molodtsov [9] (1999) introduced the concept of a soft set as a new approach for modeling uncertainties. After that Maji et al. [7] established some fundamental operations between two soft sets and then tackled one of their applications in decision making problems. Shabir and Naz(2011)[11] studied the topological structures of soft sets.

Selvanayaki et. al. [10] introduced αgrw -closed sets in soft topological spaces. In this paper we study some more properties of soft αgrw -closed sets.

Definition 1.1. [9] *Let U be an initial universe set and E be a set of parameters. Let $P(U)$ denotes the power set of U and $A \subseteq E$. A pair (F, A) is called a soft set over U , where F is a mapping given by $F : A \rightarrow P(U)$.*

Definition 1.2. [8] *Let U be an universal set and E be an universe set of parameters. Let (F, A) and (G, B) be soft sets over a common universe set U and $A, B \subseteq E$. Then (F, A) is a subset of (G, B) , denoted by $(F, A) \subseteq (G, B)$, if*

(i) $A \subseteq B$,

(ii) for all $e \in E$, $F(e) \subseteq G(e)$.

(F, A) equals (G, B) , denoted by $(F, A) = (G, B)$, if $(F, A) \tilde{\subseteq} (G, B)$ and $(G, B) \tilde{\subseteq} (F, A)$.

We denote the family of these soft sets by $SS(X)_E$.

Definition 1.3. [8] *Two soft set (F, A) and (G, B) over a common universe U are said to be equal if (F, A) is a soft subset of (G, B) and (G, B) is a soft subset of (F, A) .*

Definition 1.4. [8] *A soft set (F, A) over U is said to be a null soft set, denoted by $\tilde{\phi}$, if $\forall \epsilon \in A, F(\epsilon) = \phi$.*

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Definition 1.5. [8] A soft set (F, A) over U is said to be a absolute soft set, denoted by \tilde{U} , if $\forall e \in A, F(e) = U$,

Definition 1.6. [8] Union of two soft sets of (F, A) and (G, B) over the common universe U is the soft set (H, C) , where $C = A \cup B$, and $\forall e \in C$,

$$H(e) = \begin{cases} F(e), & \text{if } e \in A - B \\ G(e), & \text{if } e \in B - A \\ F(e) \cup G(e), & \text{if } e \in A \cap B \end{cases}$$

Definition 1.7. [8] Intersection of two soft sets (F, A) and (G, B) over the common universe U is the soft set (H, C) , where $C = A \cap B$, and $\forall e \in C, H(e) = F(e) \text{ or } G(e)$. We write $(F, A) \tilde{\cap} (G, B) = (H, C)$.

Definition 1.8. [2] The complement of a soft set (F, A) , denoted by $(F, A)^c$, is defined by $(F, A)^c = (F^c, A)$, $F^c : A \rightarrow P(X)$ is mapping given by $F^c(e) = X - F(e), \forall e \in A$ and F^c is called the soft complement function of F .

Definition 1.9. [8] A soft set (E, A) over X is said to be soft element if there exists $\alpha \in A$ such that $E(\alpha)$ is a singleton, say $\{x\}$, and $E(\beta) = \phi, \forall \beta (\neq \alpha) \in A$, such a soft element is denoted by E_α^x .

Definition 1.10. [11] Let $\tilde{\tau}$ be the collection of soft sets over X . Then $\tilde{\tau}$ is said to be a soft topology on X if

(i) $(\tilde{\phi}, A), (\tilde{X}, A) \in \tilde{\tau}$, where $\tilde{\phi}(\alpha) = \phi$ and $\tilde{X}(\alpha) = X, \forall A$,

(ii) the intersection of any two soft sets in $\tilde{\tau}$ belongs to $\tilde{\tau}$,

(iii) the union of any number of soft sets in $\tilde{\tau}$ belongs to $\tilde{\tau}$.

The triple $(X, \tilde{\tau}, A)$ is called a soft topological space over X . The members of $\tilde{\tau}$ are said to be soft open sets in X .

Definition 1.11. Let $(X, \tilde{\tau}, E)$ be a soft topological space over X and (A, E) be a soft set in $(X, \tilde{\tau}, E)$ is called

(a) soft regular open [13] $(A, E) = \text{int}_s(\text{cl}_s(A, E))$ and soft regular closed $(A, E) \cong \text{cl}_s(\text{int}_s(A, E))$.

(b) soft α -open [1] $(A, E) \tilde{\subseteq} \text{int}_s(\text{cl}_s(\text{int}_s(A, E)))$ and soft α -closed if $\text{cl}_s(\text{int}_s(\text{cl}_s(A, E))) \tilde{\subseteq} (A, E)$.

Definition 1.12. [14] In a soft topological space $(X, \tilde{\tau}, E)$, a soft set (G, C) is said to be regular semi-open soft set if there is a regular open soft set (H, B) such that $(H, B) \tilde{\subseteq} (G, C) \tilde{\subseteq} \text{cl}_s(H, B)$

Definition 1.13. A soft set (A, E) of a soft topological space $(X, \tilde{\tau}, E)$ is called

(a) a soft generalized closed (briefly soft g-closed) [6] if $\text{cl}_s(A, E) \tilde{\subseteq} (U, E)$ whenever $(A, E) \tilde{\subseteq} (U, E)$ and (U, E) is soft open in $(X, \tilde{\tau}, E)$,

(b) a soft α -generalized closed (briefly soft α g-closed)[3] if $\alpha \text{cl}_s(A, E) \tilde{\subseteq} (U, E)$ whenever $(A, E) \tilde{\subseteq} (U, E)$ and (U, E) is soft open in $(X, \tilde{\tau}, E)$.

Definition 1.14. [10] A soft set (A, E) in a soft topological space $(X, \tilde{\tau}, E)$ is called a soft α -generalized regular weakly closed (briefly soft α grw-closed) set in $(X, \tilde{\tau}, E)$ if $\alpha cl_s(A, E) \tilde{\subseteq} (U, E)$ whenever $(A, E) \tilde{\subseteq} (U, E)$ and (U, E) is soft regular semi open in $(X, \tilde{\tau}, E)$.

Definition 1.15. [5] Let $(X, \tilde{\tau}, E)$ be a soft topological space, $(F, E), (G, E)$ be semi closed sets in X such that $(F, E) \tilde{\cap} (G, E) = \tilde{\phi}$. If there exist semi open soft sets (F_1, E) and (F_2, E) such that $(F, E) \tilde{\subseteq} (F_1, E), (G, E) \tilde{\subseteq} (F_2, E)$ and $(F_1, E) \tilde{\cap} (F_2, E) = \tilde{\phi}$, then $(X, \tilde{\tau}, E)$ is called a soft semi normal space.

Definition 1.16. [4] A soft topological space $(X, \tilde{\tau}, E)$ is said to be soft compact if every soft open cover of (X, E) has a finite subcover.

Definition 1.17. [12] Let $(X, \tilde{\tau}, E)$ be a soft topological space over $X, (G, A)$ a soft closed set in $(X, \tilde{\tau}, E)$ and $e_F \tilde{\in} X_A$ such that $e_F \tilde{\notin} (G, A)$. If there exist soft open sets (F_1, A) and (F_2, A) such that $e_F \tilde{\in} (F_1, A), (G, A) \tilde{\subseteq} (F_1, A) \tilde{\cap} (F_2, A) = \phi_A$, then $(X, \tilde{\tau}, E)$ is called a soft regular space.

2 Soft α grw-closed sets in soft topological spaces

Proposition 2.1. In a soft topological space $(X, \tilde{\tau}, E)$, $RSOSS(X, \tilde{\tau}, E) = \{\tilde{\phi}, \tilde{X}\}$, where $RSOSS(X, \tilde{\tau}, E)$ is the set of all soft regular semi-open sets, then every subset of $SS(X)_E$ is soft α grw-closed.

Proof. Assume that $RSOSS(X, \tilde{\tau}, E) = \{\tilde{\phi}, \tilde{X}\}$ and (A, E) be any subset of $SS(X)_E$. Suppose $(A, E) = \tilde{\phi}$, then (A, E) is a soft α grw-closed set. Suppose $(A, E) \neq \tilde{\phi}$, then \tilde{X} is the only soft regular semi-open set containing (A, E) and so $\alpha cl_s((A, E)) \tilde{\subseteq} \tilde{X}$. Hence (A, E) is soft α grw-closed.

Remark 2.2. The converse of the above proposition need not be true as seen from the following example.

Example 2.3. Let $X = \{x_1, x_2, x_3\}, E = \{e_1, e_2\}$ and $\tilde{\tau} = \{\tilde{\phi}, \tilde{X}, (F_1, E), (F_2, E), (F_3, E), (F_4, E), (F_5, E), (F_6, E)\}$ where $(F_1, E), (F_2, E), (F_3, E), (F_4, E), (F_5, E), (F_6, E)$ are soft sets over X defined as follows

$$\begin{aligned} F_1(e_1) &= \{x_1\}, & F_1(e_2) &= \{x_1\}, \\ F_2(e_1) &= \{x_2\}, & F_2(e_2) &= \{x_2\}, \\ F_3(e_1) &= \{x_3, x_2\}, & F_3(e_2) &= \{x_3, x_2\}, \\ F_4(e_1) &= \{x_1, x_2\}, & F_4(e_2) &= \{x_1, x_2\} \\ F_5(e_1) &= \{x_2, x_3\}, & F_5(e_2) &= \{x_2, x_3\} \\ F_6(e_1) &= \{x_1, x_3\}, & F_6(e_2) &= \{x_1, x_3\}. \end{aligned}$$

In $(X, \tilde{\tau}, E)$, every subset of (X, E) is soft α grw-closed but $RSOSS(X, E) \neq \{\tilde{\phi}, \tilde{X}\}$.

Proposition 2.4. Every subset of $SS(X)_E$ is soft α grw-closed if and only if $RSOSS(X, \tilde{\tau}, E) \tilde{\subseteq} \{(F, E) \tilde{\subseteq} SS(X)_E \mid (F^c, E) \tilde{\in} S\alpha OS(X, \tilde{\tau}, E)\}$, where $S\alpha OS(X, \tilde{\tau}, E)$ is the set of all soft α -open sets in $(X, \tilde{\tau}, E)$.

Proof. Suppose that every soft subset of $SS(X)_E$ is soft α grw-closed. Let $(U, E) \tilde{\in} ROSS(X, \tilde{\tau}, E)$. Since $(U, E) \tilde{\subseteq} (U, E)$ and (U, E) is soft regular semi-open, $\alpha cl_s((U, E)) \tilde{\subseteq} (U, E)$. Thus $(U, E) \tilde{\in} \{(F, E) \tilde{\subseteq} (X, E) \mid (F^c, E) \tilde{\in} S\alpha OS(X, \tilde{\tau}, E)\}$.

Conversely, assume $RSOSS(X, \tilde{\tau}, E) \tilde{\subseteq} \{(F, E) \tilde{\subseteq} (X, E) : (F^c, E) \tilde{\in} S\alpha OS(X, \tilde{\tau}, E)\}$. Let (A, E) be any subset of $SS(X)_E$ such that $(A, E) \tilde{\subseteq} (U, E)$, where (U, E) is soft regular semi-open. Thus (U, E) is soft α -closed and so $\alpha cl_s((A, E)) \tilde{\subseteq} (U, E)$. Hence (A, E) is soft α grw-closed.

Proposition 2.5. *If (A, E) is both soft open and soft g -closed in $(X, \tilde{\tau}, E)$, then (A, E) is soft α grw-closed $(X, \tilde{\tau}, E)$.*

Proof. Let $(A, E) \subseteq (U, E)$ and (U, E) be soft regular semi-open. Now $(A, E) \subseteq (A, E)$ and so $cl_s((A, E)) \subseteq (A, E)$, because (A, E) is soft open and soft g -closed. This implies $\alpha cl_s((A, E)) \subseteq cl_s(A, E) \subseteq (U, E)$ since every soft closed is soft α -closed. Hence (A, E) is soft α grw-closed.

Remark 2.6. *If (A, E) is soft α grw-closed in $(X, \tilde{\tau}, E)$, then (A, E) need not be soft open and soft g -closed $(X, \tilde{\tau}, E)$.*

Example 2.7. *Let $X = \{x_1, x_2\}$, $E = \{e_1, e_2\}$ and $\tilde{\tau} = \{ \tilde{\phi}, \tilde{X} (F_1, E), (F_2, E), (F_3, E), (F_4, E) \}$ where $(F_1, E), (F_2, E), (F_3, E), (F_4, E)$ are soft sets over X , defined as follows $F_1(e_1) = \{x_2\}$, $F_1(e_2) = \{x_1\}$,
 $F_2(e_1) = \{x_1\}$, $F_2(e_2) = \{x_2\}$,
 $F_3(e_1) = \{\phi\}$, $F_1(e_2) = \{x_1\}$,
 $F_4(e_1) = \{x_1\}$, $F_3(e_2) = \{X\}$.*

Then a soft set (A, E) such that $A(e_1) = \{x_1\}$, $A(e_2) = \{x_1\}$ is both soft open and soft α grw-closed but not soft g -closed.

Proposition 2.8. *If (A, E) is soft regular semi-open and soft α grw-closed, then (A, E) is soft α -closed.*

Proof. Suppose (A, E) is soft regular semi-open and soft α grw-closed, $\alpha cl_s((A, E)) \subseteq (A, E)$. Also $(A, E) \subseteq \alpha cl_s((A, E))$, so $\alpha cl_s((A, E)) = (A, E)$. Hence (A, E) is soft α -closed.

Remark 2.9. *In Example 2.7, the soft set $(e_1, \{x_2\}), (e_2, \{\phi\})$ is soft α -closed and soft α grw-closed but not soft regular semi-open.*

Corollary 2.10. *Let (A, E) be soft regular semi-open and soft α grw-closed. Then $(A, E) \tilde{\cap} (F, E)$ is soft α grw-closed for every soft α -closed set (F, E) .*

Proof. Since (A, E) is soft regular semi-open and soft α grw-closed, then by Proposition 2.8, (A, E) is soft α -closed. Therefore $(A, E) \tilde{\cap} (F, E)$ is soft α -closed, since (F, E) is soft α -closed. Hence $(A, E) \tilde{\cap} (F, E)$ is soft α grw-closed.

Proposition 2.11. *If (A, E) is both soft open and soft α g-closed, then (A, E) is soft α grw-closed.*

Proof. Suppose (A, E) is both soft open and soft α g-closed. Let $(A, E) \subseteq (U, E)$ and (U, E) is soft regular semi-open. Now $(A, E) \subseteq (A, E)$ and by hypothesis $\alpha cl_s((A, E)) \subseteq (A, E)$. Therefore $\alpha cl_s((A, E)) \subseteq (U, E)$. Hence (A, E) is soft α grw-closed.

Remark 2.12. *If (A, E) is both soft open and soft α grw-closed, then (A, E) need not be α g-closed. In Example 2.7, the soft subset $A(e_1) = \{\phi\}$, $A(e_2) = \{X\}$ is soft α grw-closed but not soft open and not soft α g-closed.*

Remark 2.13. *Difference of two soft α grw-closed sets is not generally soft α grw-closed.*

Example 2.14. *Let $X = \{x_1, x_2\}$, $E = \{e_1, e_2\}$ and $\tilde{\tau} = \{ \tilde{\phi}, \tilde{X}, (F_1, E), (F_2, E), (F_3, E) \}$ where $(F_1, E), (F_2, E), (F_3, E)$ are soft sets over (X, E) , defined as follows
 $F_1(e_1) = \{\phi\}$, $F_1(e_2) = \{x_1\}$,
 $F_2(e_1) = \{x_1\}$, $F_2(e_2) = \{x_2\}$,
 $F_3(e_1) = \{x_1\}$, $F_3(e_2) = \{X\}$.*

Then the soft sets $(A, E) = \{(e_1, \{X\}), (e_2, \{x_2\})\}$ and $(B, E) = \{(e_1, \{x_2\}), (e_2, \{x_1\})\}$ are soft α grw-closed but $(A, E) - (B, E) = \{(e_1, \{x_1\}), (e_2, \{x_2\})\}$ is not soft α grw-closed.

Definition 2.15. The intersection of all soft regular semi-open subsets of $(X, \tilde{\tau}, E)$ containing (A, E) is said to be the soft regular semi-kernal of (A, E) and is denoted by $srsker((A, E))$.

i.e., $srsker((A, E)) = \bigcap \{(F, E) : (A, E) \subseteq (F, E), \text{ where } (F, E) \in RSOSS(X, \tilde{\tau}, E)\}$.

Theorem 2.16. A soft subset (A, E) of $SS(X)_E$ is soft αgrw -closed if and only if $\alpha cl_s((A, E)) \subseteq srsker((A, E))$.

Proof. Consider (A, E) is soft αgrw -closed. Let $X_e^x \notin \alpha cl_s((A, E))$, where X_e^x is a soft element of $SS(X)_E$. Suppose that $X_e^x \notin srsker((A, E))$, then there is a soft regular semi-open set (U, E) containing (A, E) such that $X_e^x \notin (U, E)$. Since (U, E) is soft regular semi-open containing (A, E) , we have $X_e^x \notin \alpha cl_s((A, E))$, which is a contradiction. Thus $\alpha cl_s((A, E)) \subseteq srsker((A, E))$.

Conversely, let $\alpha cl_s((A, E)) \subseteq srsker(A, E)$ and (U, E) be soft regular semi-open such that $(A, E) \subseteq (U, E)$, then $\alpha cl_s((A, E)) \subseteq srsker(A, E) \subseteq (U, E)$. Therefore (A, E) is soft αgrw -closed.

Proposition 2.17. Let $(X, \tilde{\tau}, E)$ be a soft regular space in which every soft regular semi-open subset is soft open. If (A, E) is soft compact subset of $(X, \tilde{\tau}, E)$, then (A, E) is soft αgrw -closed.

Proof. Let $(A, E) \subseteq (U, E)$ and (U, E) be soft regular semi-open. By assumption (U, E) is soft open in $(X, \tilde{\tau}, E)$. Since (A, E) is a soft compact subset of a soft regular space $(X, \tilde{\tau}, E)$, then there exists a soft closed set (V, E) such that $(A, E) \subseteq (V, E) = cl_s((V, E)) \subseteq (U, E)$. Thus $\alpha cl_s((A, E)) \subseteq (U, E)$. Hence (A, E) is soft αgrw -closed.

Proposition 2.18. If $(X, \tilde{\tau}, E)$ is soft semi-normal and $(F, E) \cap (A, E) = \phi$, where (F, E) is soft regular semi-open and (A, E) is soft αgrw -closed, then there exist disjoint soft semi open sets (S_1, E) and (S_2, E) such that $(A, E) \subseteq (S_1, E)$ and $(F, E) \subseteq (S_2, E)$.

Proof. Since (F, E) is soft regular semi open and $(F, E) \cap (A, E) = \phi$. Then $(A, E) \subseteq (F^c, E)$ and so $\alpha cl_s((A, E)) \subseteq (F^c, E)$. Thus $\alpha cl_s((A, E)) \cap (F, E) = \phi$. Since $\alpha cl_s((A, E))$ and (F, E) are soft semi closed and $(X, \tilde{\tau}, E)$ is soft semi normal, there exist disjoint soft semi open sets (S_1, E) and (S_2, E) such that $\alpha cl_s((A, E)) \subseteq (S_1, E)$ and $(F, E) \subseteq (S_2, E)$. This implies $(A, E) \subseteq (S_1, E)$ and $(F, E) \subseteq (S_2, E)$.

Proposition 2.19. If $(X, \tilde{\tau}, E)$ is soft semi-normal in which every α -closed set is closed and $(F, E) \cap (A, E) = \phi$, where (F, E) is soft regular closed and (A, E) is soft αgrw -closed then there exist disjoint soft open sets (O_1, E) and (O_2, E) such that $(A, E) \subseteq (O_1, E)$ and $(F, E) \subseteq (O_2, E)$.

Proof. Similar to Proposition 2.18.

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